

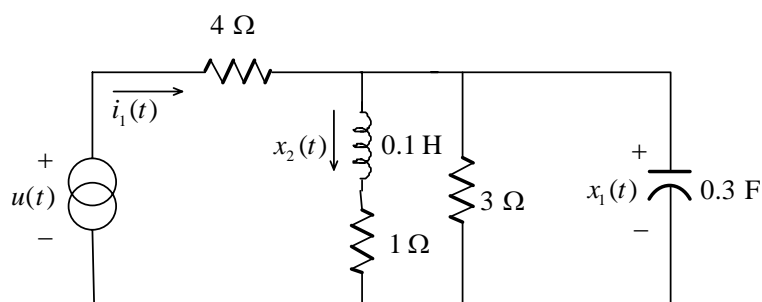


**Answer all questions:**

**Q1** - Evaluate the inverse of the given  $z$ -transform  $H(z) = \frac{z^2 + 2z}{\left(z - \frac{1}{4}\right)\left(z + \frac{1}{6}\right)^2}$  [10]  
 for the following cases:

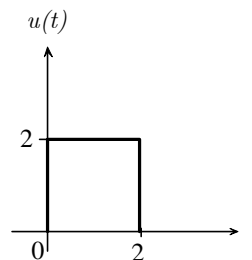
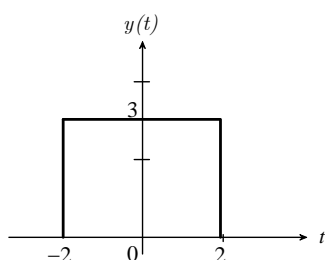
- (a) ROC  $|z| > 1/3$       (b) ROC  $1/6 < |z| < 1/4$   
 (c) ROC  $|z| > 4$       (d) ROC  $|z| < 1/8$

**Q2** - Write a state - variable description for the circuit shown below, find the impulse response, then verify if the system is stable or not. [10]



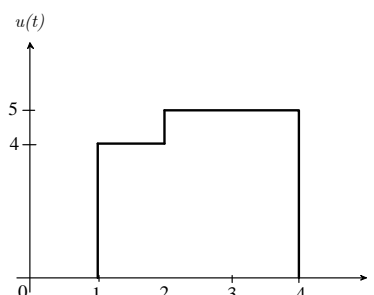
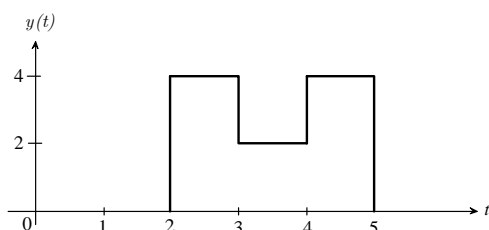
**Q3** – When the input to a continues-time system  $\mathcal{X}(t)$  the output is the shown  $y(t)$ , find the output of the same system to the given input signal  $u(t)$  for [10]

(a)



[5]

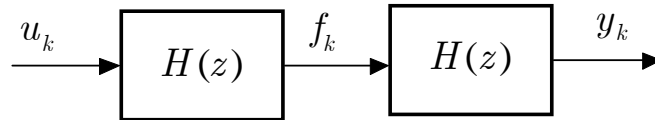
(b)



[5]

**Q4** - Two identical systems with the transfer function  $\{h_k\} = (1/5)^k, k \geq 0$ . The two systems are cascaded as shown. If the sequence  $f_k$  has the Z- transform

$$F(z) = \frac{z^3 + z^2}{\left(z - \frac{1}{2}\right)\left(z - \frac{1}{3}\right)^2}$$



(a) Find the sequences  $u_k$ . [5]

(b) Find the sequences  $y_k$ . [5]